



## Application of Neural Networks in LS-OPT: Parametric Study and Guidelines

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3<sup>rd</sup> German LS-DYNA Users Meeting  
Bamberg, Germany  
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### Overview

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- **Metamodeling Methods**
  - Goals
- **Optimization**
  - Technologies
- **Examples**
  - Frontal Crash: full vehicle
  - Knee Impact
  - Analytical Benchmarks
- **Conclusion**

## How are metamodels used in crash ?

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- **Surrogate model for design**
  - Approximations critical for design modeling in nonlinear dynamics (LS-DYNA)
  - Global approximation: Optimization & Tradeoff
- **Model for any number of simulation runs**
  - Given: number of simulation runs
  - Required: Surrogate model
  - Different polynomial orders require discrete numbers of runs (e.g. 10var: L=11+, Q=66+)
  - Adding points to a simple model (linear) does not significantly improve the prediction accuracy
- **Local improvement**
  - Refine regionally, but maintain global relevance

## Technologies for Optimization

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- **Metamodels**
  - Response Surface Methodology
  - Feedforward Neural Networks
- **Point selection:**
  - RSM: *D*-Optimal
  - NN: Updated Space Filling (Maximize Min. Distance between any two points) Johnson (1990)
- **Subdomain Reduction**
  - Reduce the region of interest for each iteration
  - Heuristics: Roux/Stander *et al* (*MA&O* 1996, *IJNME* 1998, Crash & Benchmarking: *EC* 2002)
  - RSM: Necessary for low order polynomials: regional approximation
  - NN: Necessary for regional refinement. Start with full design space
- **Simulation (LS-OPT)**
  - Parallel or distributed
  - Automated

## Metamodeling Methodology

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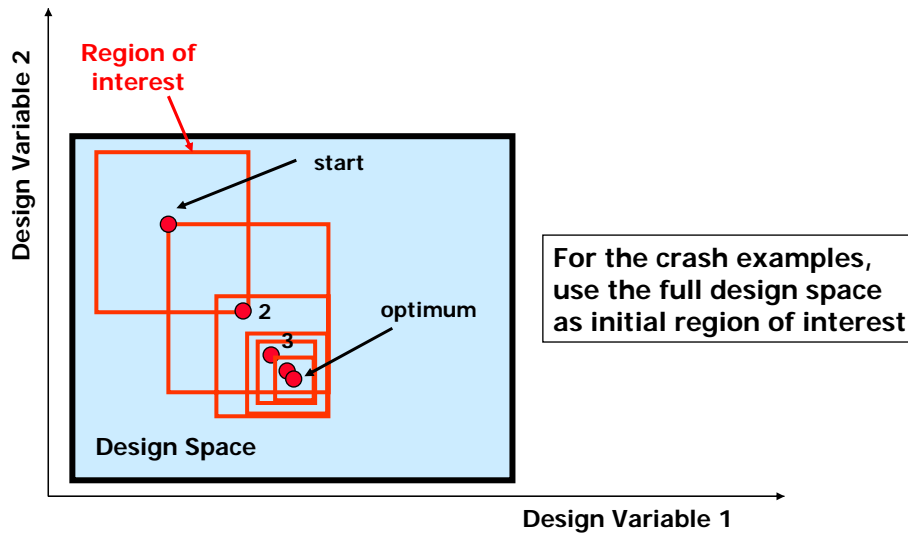
- **Response Surface Methodology (RSM)**
  - Polynomial-based (only linear in this study)
  - Point selection: D-Optimality
  - Regional (midrange) approximation
- **Neural Nets**
  - Simulation of a biological network
  - Nonlinear Regression (Levenberg-Marquardt, BFGS,...)
  - Point Selection: Updated Space Filling

## Point Selection

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- **NN**
  - Space Filling
  - Simulated Annealing to locate new points
  - Max. Min. distance between
    - new points
    - new points + fixed points
  - New points bounded by sub-region
  - **1.5(n+1)** points per iteration: relatively sparse
- **Response Surface Method**
  - Use D-Optimality (GA)
  - linear approximations
  - **1.5(n+1)** points per iteration

### Successive Approximation Scheme Converges to an Optimum

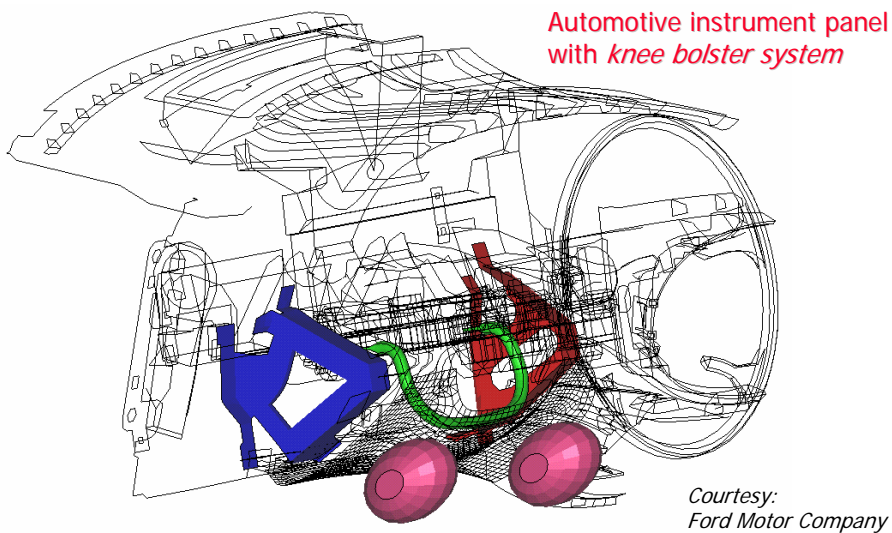


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### Components to Be Designed

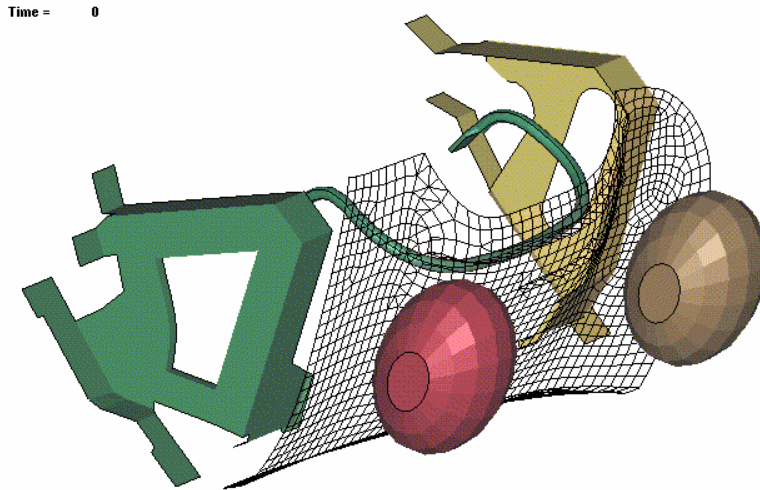


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### 40ms Impact: LS-DYNA Simulation

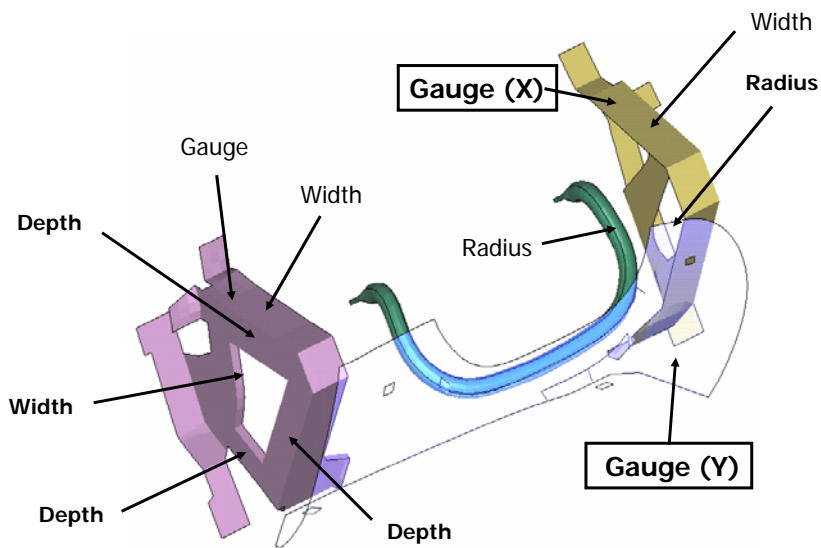


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### Two Design Variables

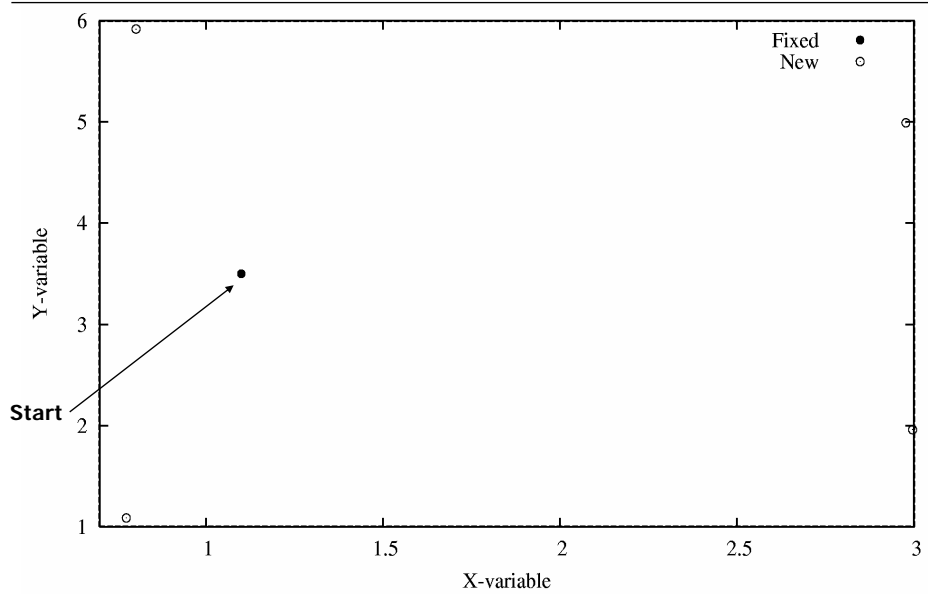


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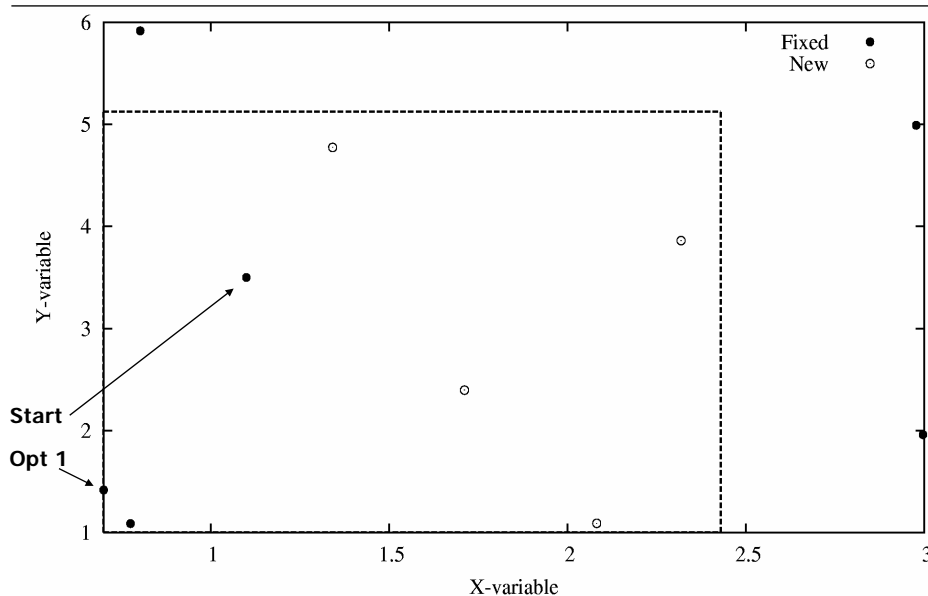
### Experimental Design: Space Filling Method Knee Impact: Iteration 1



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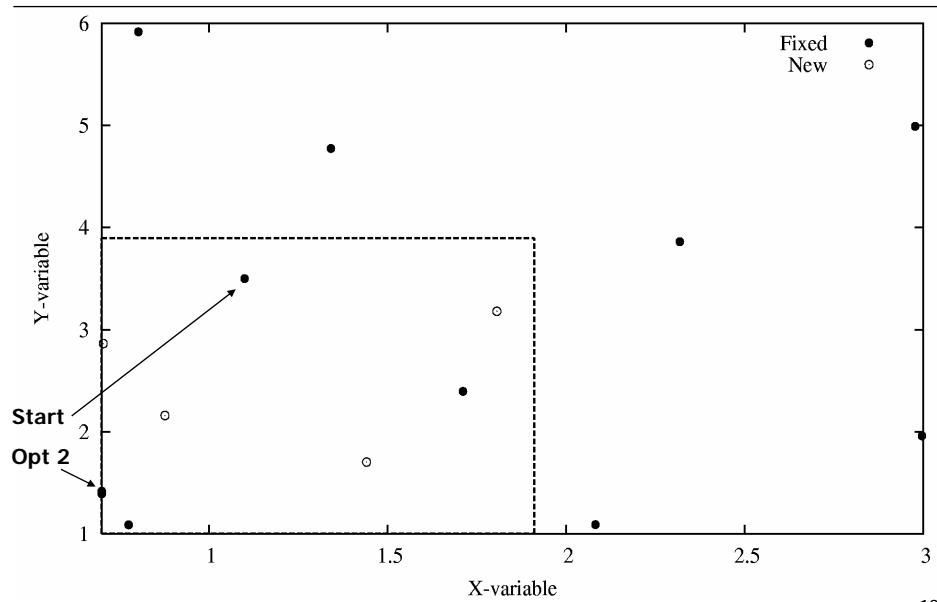
### Experimental Design: Space Filling Method Knee Impact: Iteration 2



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### Experimental Design: Space Filling Method Knee Impact: Iteration 3

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### Feedforward Neural Networks

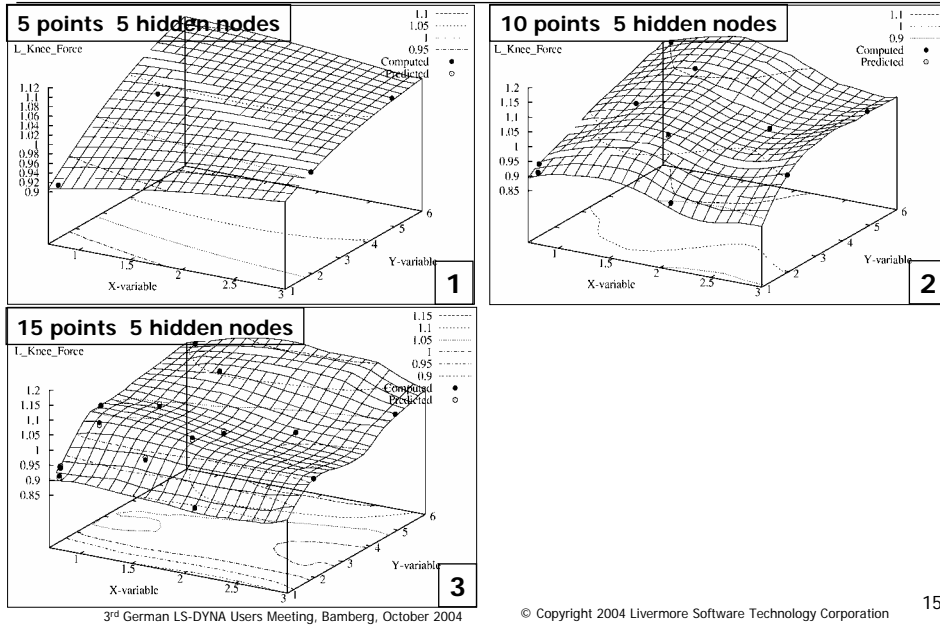
- **Construct *ensemble* of architectures (different numbers of hidden nodes)**
  - Single layer architectures (0 – 10 nodes)
  - Select the “best” net
  - Selection criterion: Min. Generalized Cross Validation (GCV)
- **Some properties of NN Variance Modeling**
  - NN's have variance due to local minima associated with training
  - Net variance is bigger for noisy functions and for extrapolation

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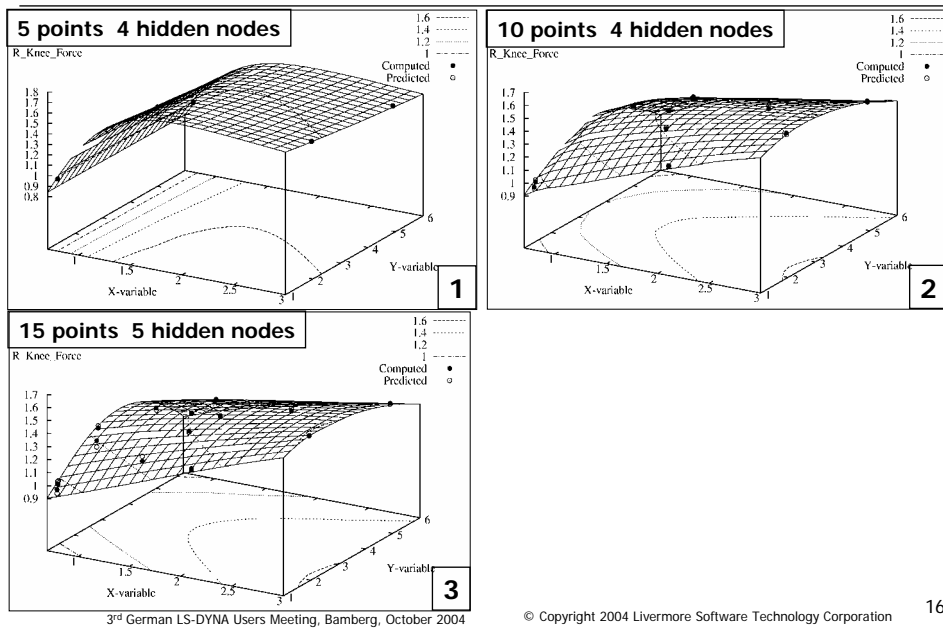
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### Neural Network Updating Knee Impact: Left Knee Force

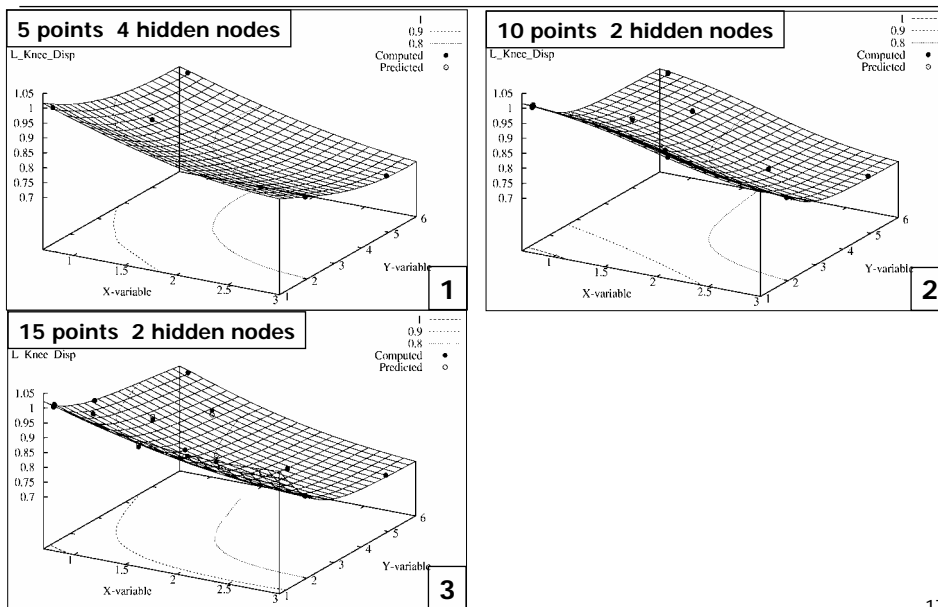


### Neural Network Updating Knee Impact: Right Knee Force





### Neural Network Updating Knee Impact: Left Knee Displacement

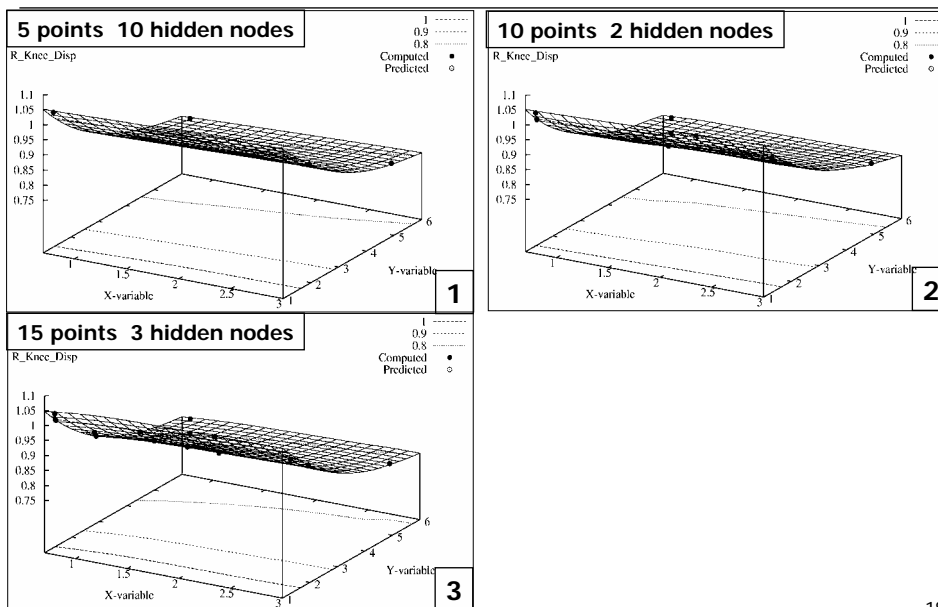


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### Neural Network Updating Knee Impact: Right Knee Displacement

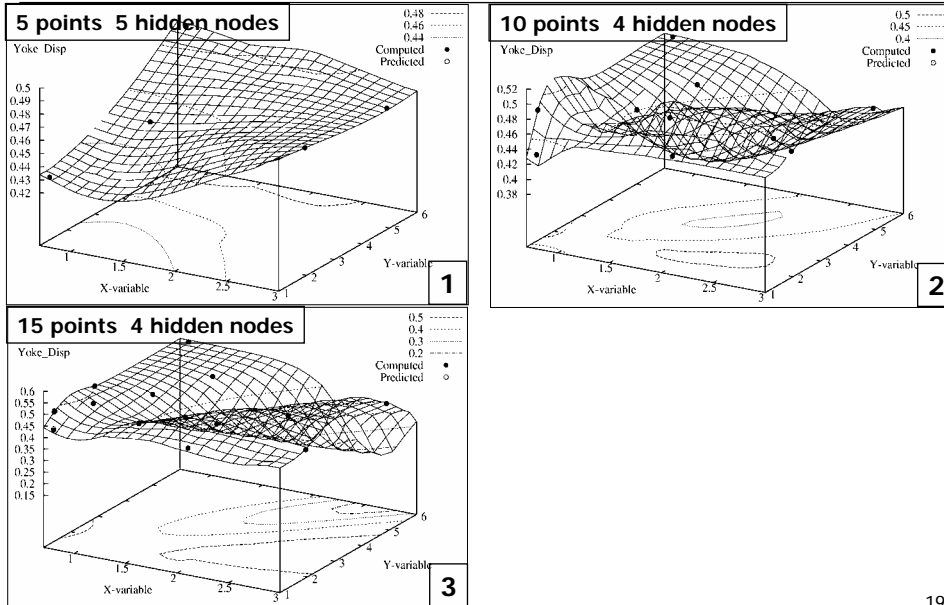


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### Neural Network Updating Knee Impact: Yoke Displacement



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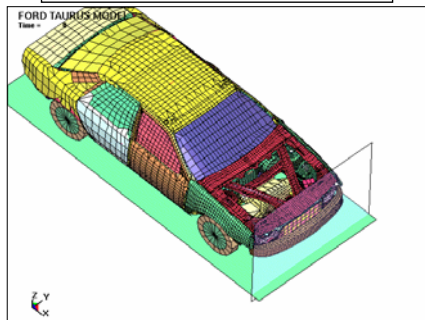
### Crash Performance of Base Design

**Crash model**

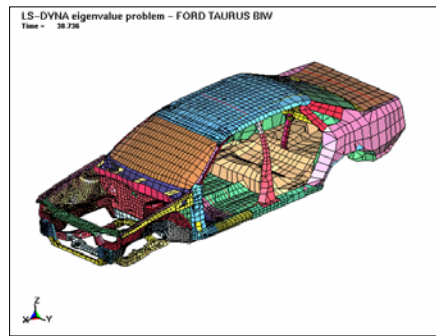
30 000 elements  
*Intrusion = 552mm*  
*Stage1Pulse = 14.34g*  
*Stage2Pulse = 17.57g*  
*Stage3Pulse = 20.76g*

**BIW model**

18 000 elements  
*Torsional mode 1*  
*Frequency = 38.7Hz*

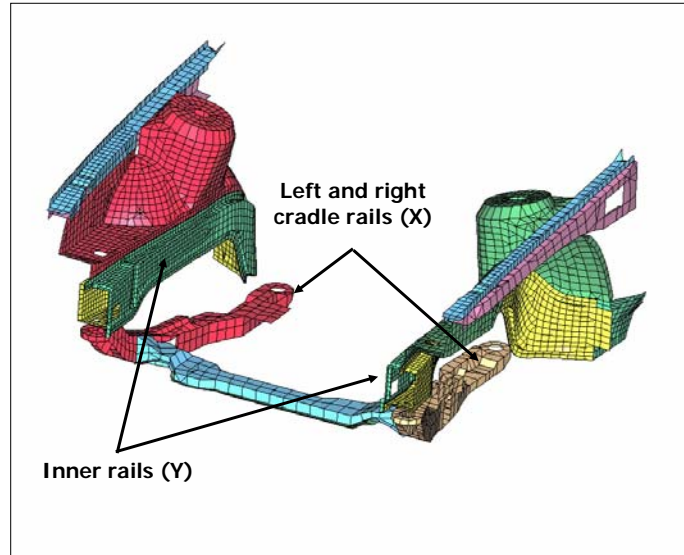


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### Two Design Variables (Thickness)

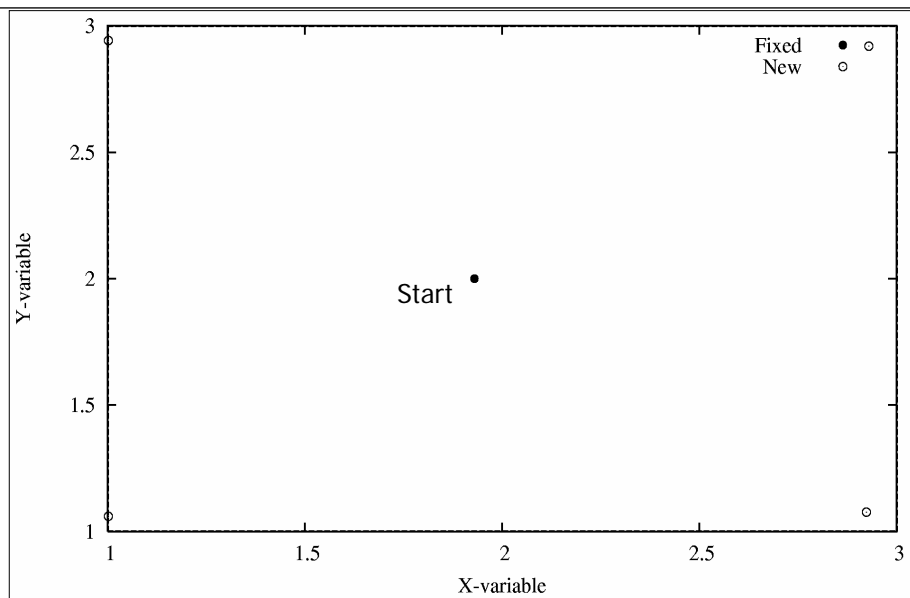


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### Experimental Design: Space Filling Method Iteration 1

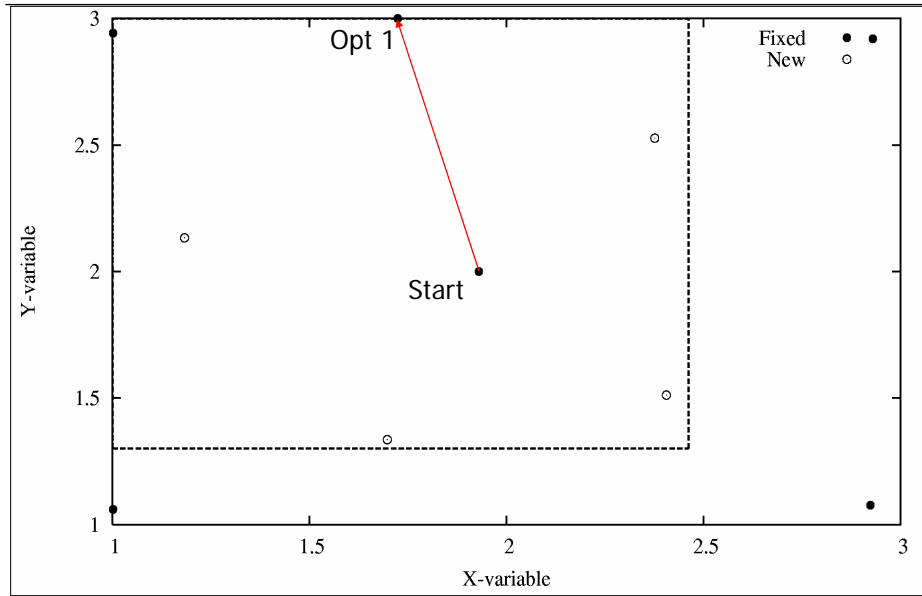


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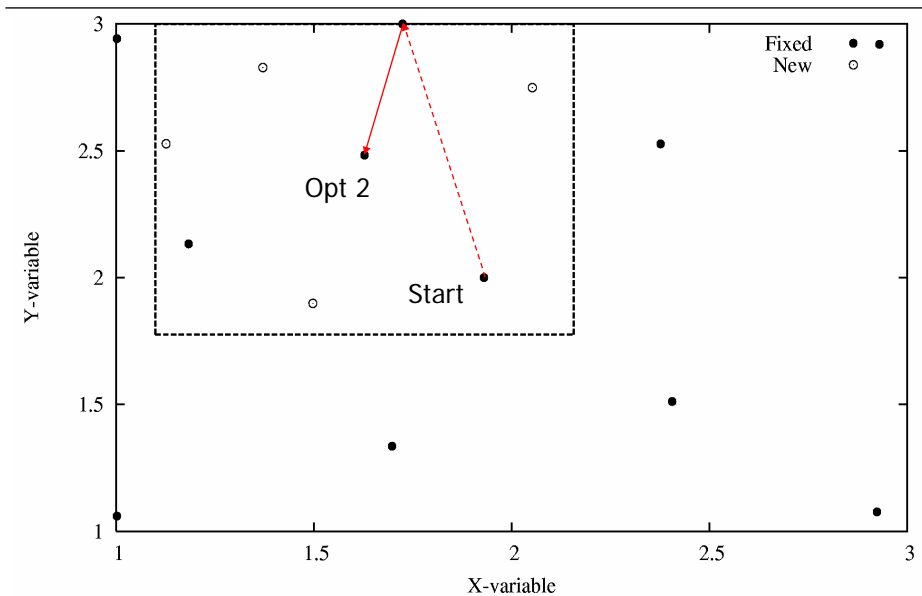
### Experimental Design: Space Filling Method Iteration 2



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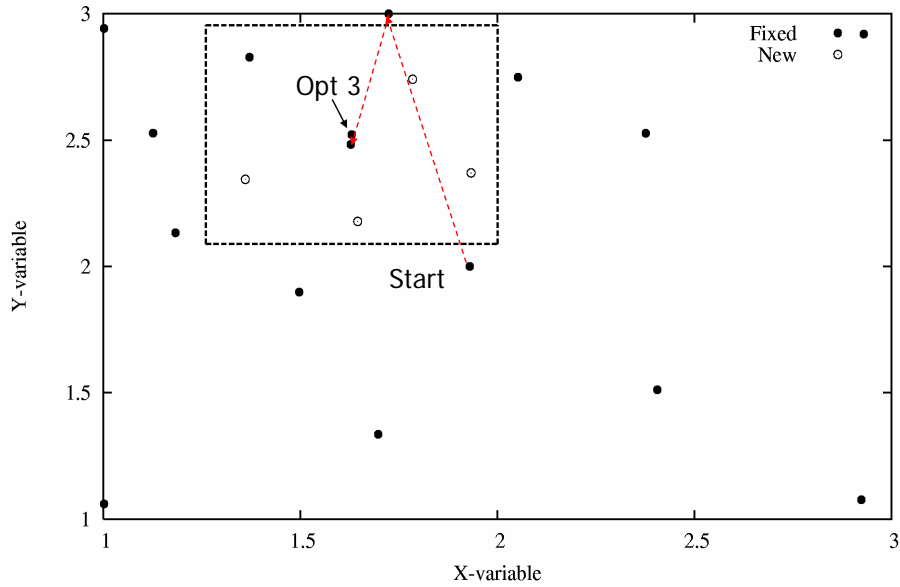
### Experimental Design: Space Filling Method Iteration 3



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### Experimental Design: Space Filling Method Iteration 4

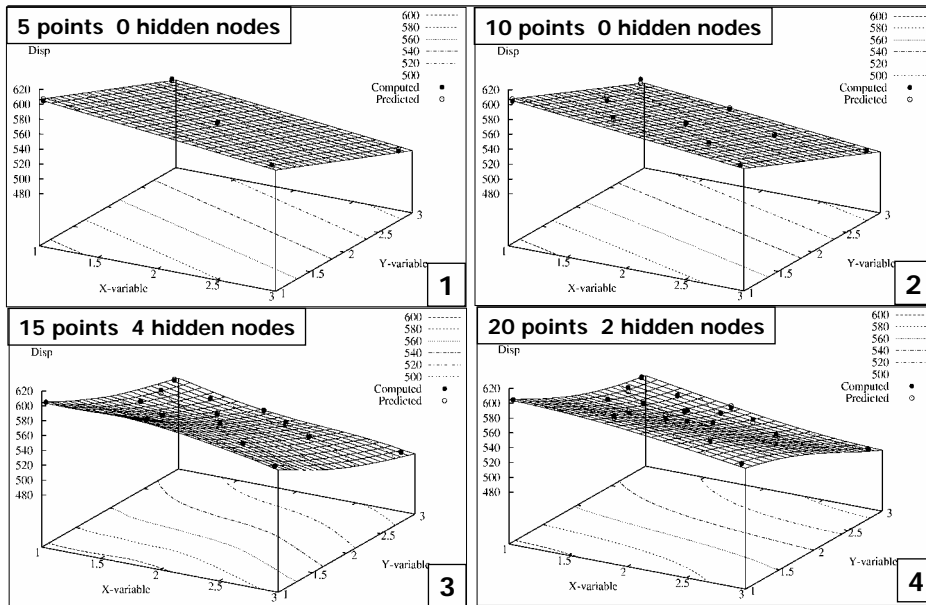


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### Neural Network Updating Vehicle Crash: Intrusion

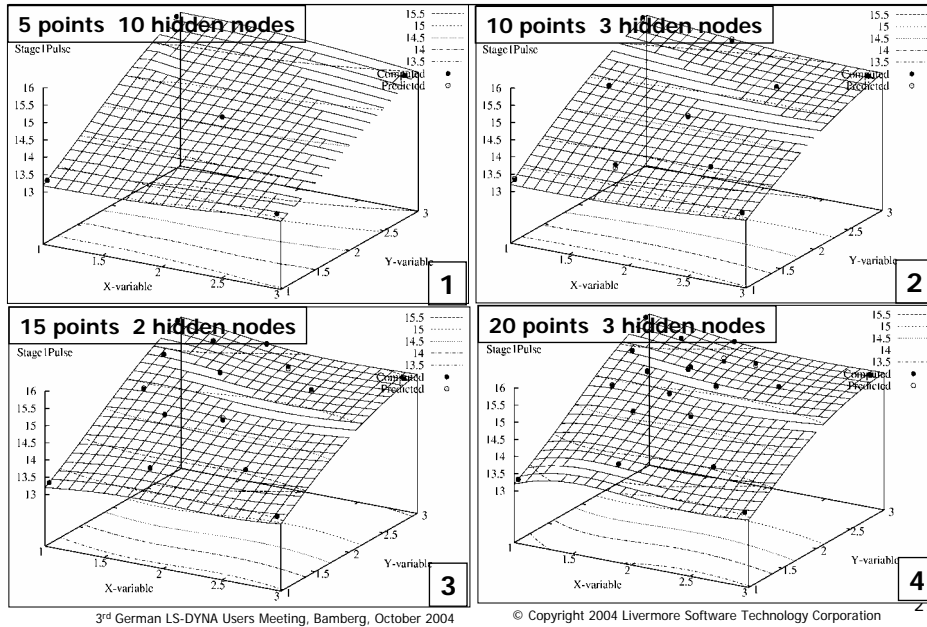


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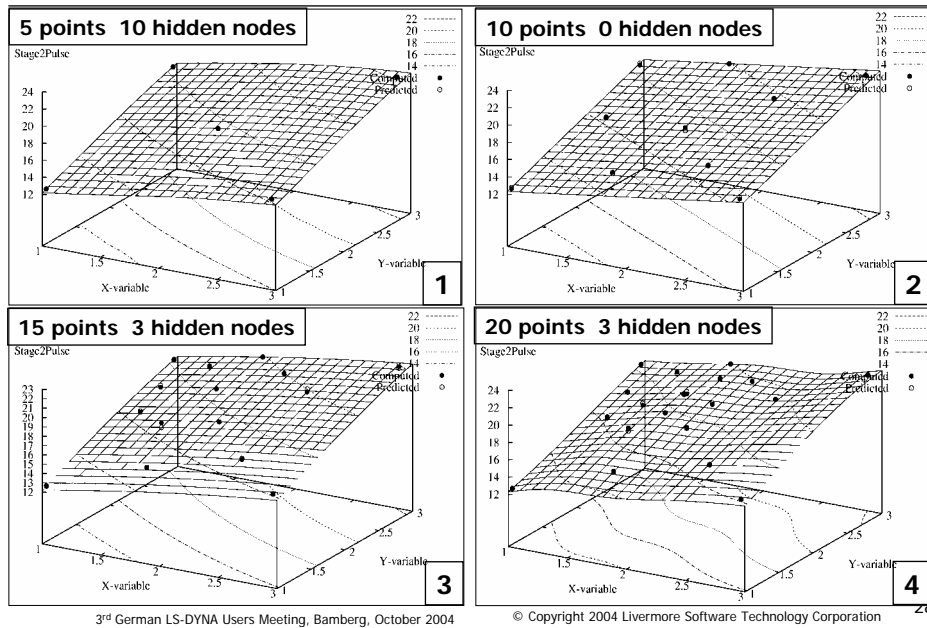
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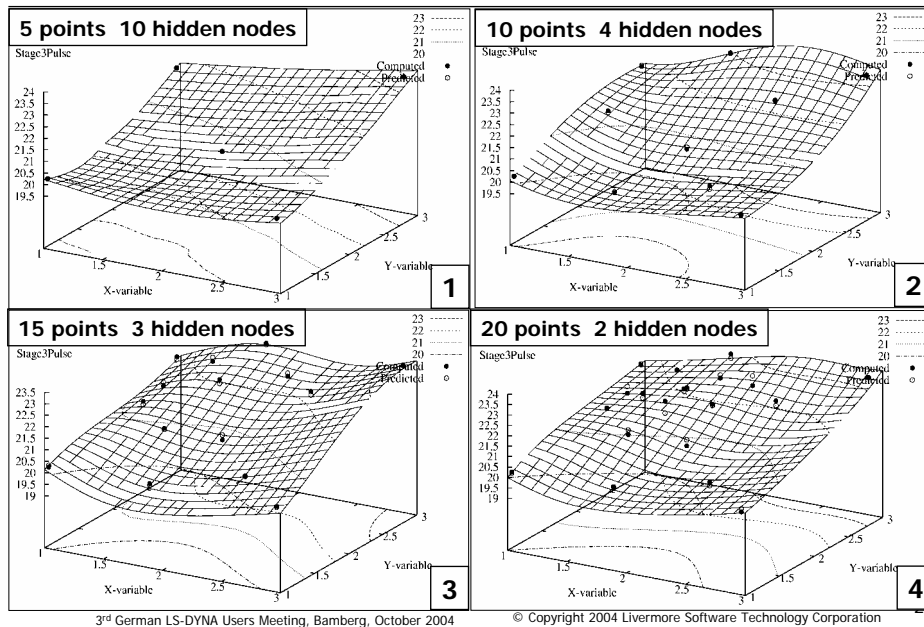
### Neural Network Updating Vehicle Crash: Stage 1 Pulse



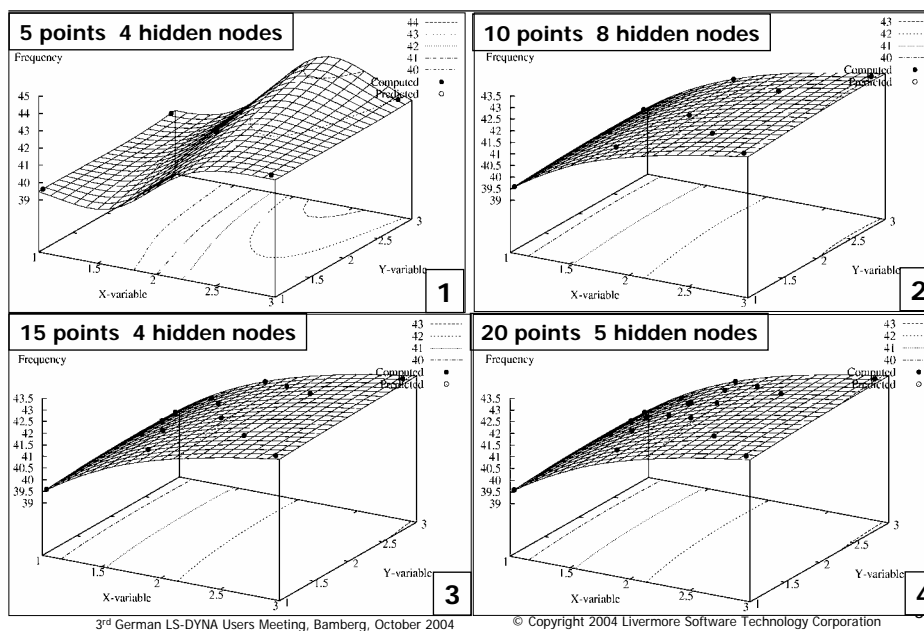
### Neural Network Updating Vehicle Crash: Stage 2 Pulse



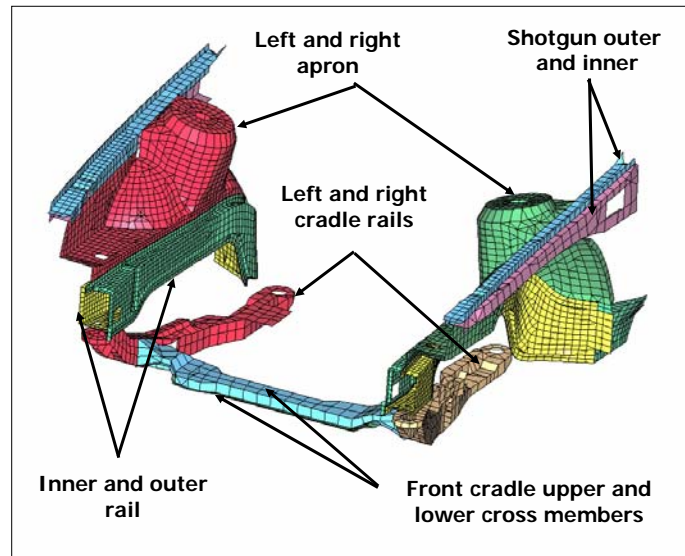
### Neural Network Updating Vehicle Crash: Stage 3 Pulse



### Neural Network Updating Torsional Mode: Frequency



## Optimization Design Variables (Thickness)



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## Design Formulation (MDF partially shared variables)

**Design Objective:**

Minimize (Mass of components)

**Design Constraints:**

Intrusion < 552.38mm

Stage1Pulse > 14.58g

Stage2Pulse > 17.47g

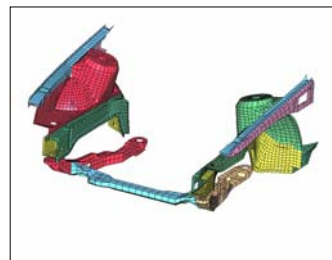
Stage3Pulse > 20.59g

41.38Hz < Torsional mode 1 frequency < 42.38

**Crashworthiness design variables: 4**

Rails (inner and outer); Aprons; Cradle rails

**NVH design variables: 7 (all)**



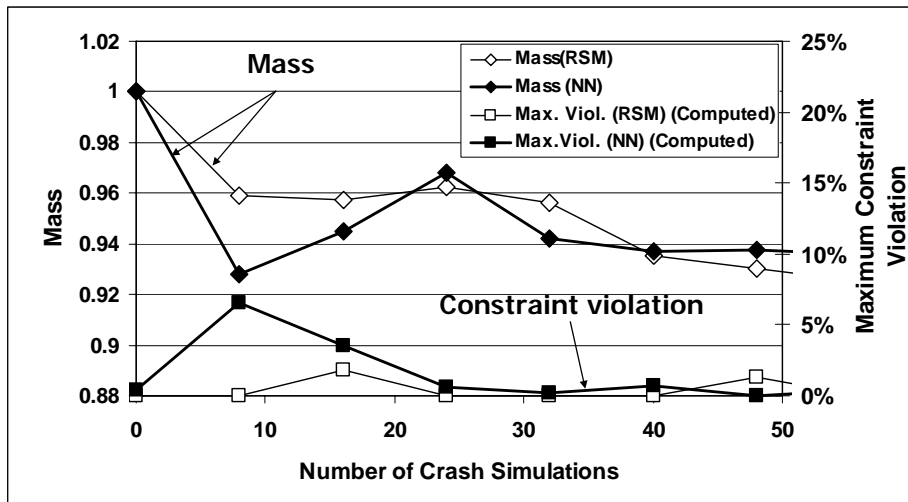
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### Full vehicle Optimization History

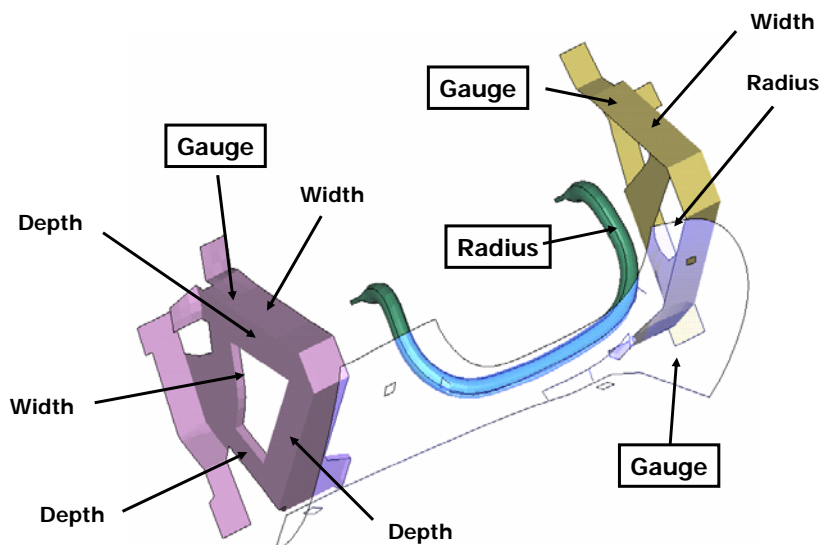


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### Design Variables



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## Design Formulation

**Design Objective:**

$$\min ( \max ( \text{Knee\_F\_L}, \text{Knee\_F\_R} ) )$$

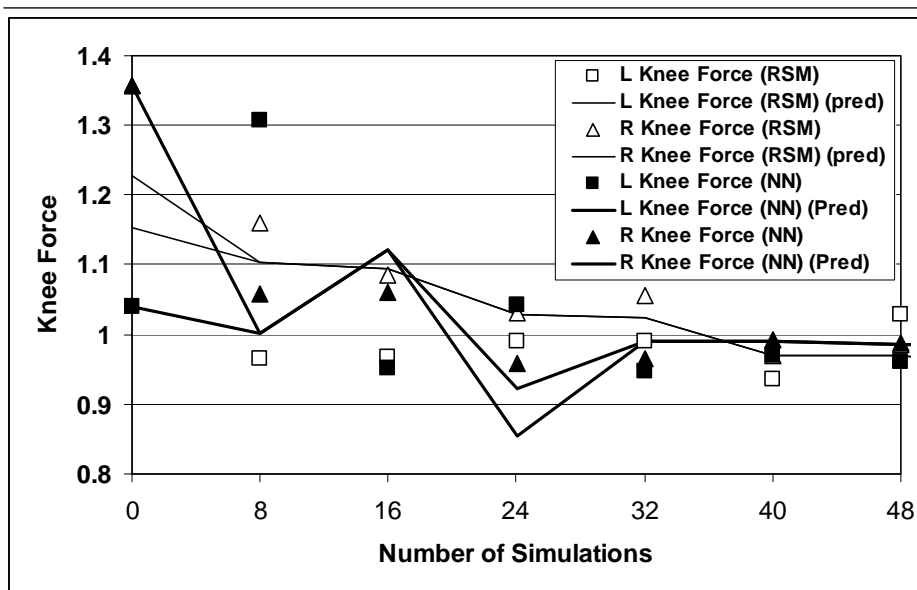
**Design Constraints:**

Left Knee intrusion	<	115mm
Right Knee intrusion	<	115mm
Yoke intrusion	<	85mm

**Design variables**

Reduced from 11 to 4 (ANOVA)

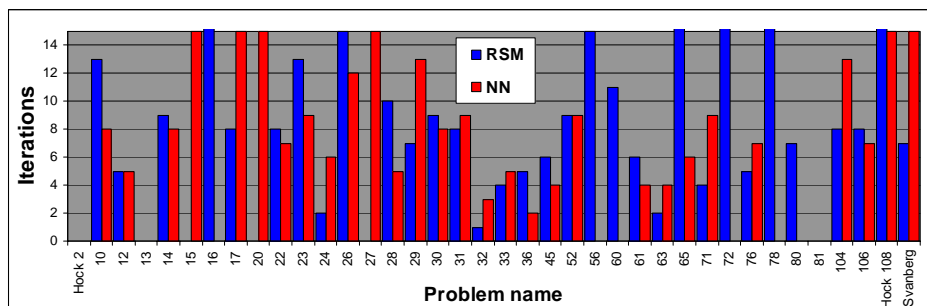
## Optimization Convergence



### Additional Benchmarks for Testing NN 37 Hock & Schittkowski, Svanberg Polytope

- Polynomials of various orders
- Exponential functions
- Svanberg Polytope (21 var.)
- 2 – 21 variables

- Number of iterations for 1% accuracy
- Omission: not converged within 15 iterations

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### Guidelines for Optimization with NN

- Use full design space as initial region of interest by simply omitting initial range (in "Variables" panel)
- Iterative updating: Use same number of points per iteration as linear response surface.
- Use Space Filling sampling method (default)
- Make sure that "Updated" Neural Net Option is set ("Sampling" panel) (default).
  - Effect: Points will be placed in Maxi-min. Positions
  - Metamodeling will be done using all available points

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## Advantages of NN

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- **Global approximation**
  - Avoids inaccuracy for small range – does regional refinement
  - Can apply trade-off study or robustness analysis after optimization run
- **Do not have to choose between different orders of polynomials.**
  - Choice of NN architectures is automated
  - Independent of number of points chosen (so can choose minimum, e.g. as for linear)
- **Do not have to choose initial range**
  - Start with full design space
- **A regression method – not interpolation**
  - Filters noise